

Sangam Skm College - Nadi

Year 12

Mathematics

Worksheet 1 - Solutions

1. Total Cost = Deposit + Installments
= \$100 + (12 x \$ 85)
= \$ 1120

2. (a) $\log 4 + \log 6 = \log (4 \times 6) = \underline{\log 24}$

(b) $\log xy + \log z = \underline{\log x y z}$

(c) $\log 2x^2 + \log x^2 - \log x = \underline{\log 2x^3}$

3. (a) $\sqrt{3} + \sqrt{12}$
 $\sqrt{3} + (\sqrt{4} \times \sqrt{3})$
 $\sqrt{3} + (2\sqrt{3})$
 $= 3\sqrt{3}$

(b) $\sqrt{27} - \sqrt{12} + \sqrt{20} - \sqrt{45}$
 $\sqrt{3} (\sqrt{9} - \sqrt{4}) + \sqrt{5} (\sqrt{4} - \sqrt{9})$
 $\sqrt{3} (3 - 2) + \sqrt{5} (2 - 3)$
 $= \sqrt{3} - \sqrt{5}$

4.

x	0	1	2	3
0	0	0	0	0
1	0	1	2	3
2	0	2	0	2
3	0	3	2	1

The above system is not a group because all elements do not have a unique Inverse.

5. (a) $2^{5m} \times 2^{3m} = 2^{8m}$

(b) $(3x^3)^2 = 9x^6$

(c) $\left(\frac{16}{25}\right)^{-1/2} = \frac{5}{4}$

6. (a) $\frac{16^{n+2} \times 2^n}{2^{5n+3}}$

(b) $\frac{2^{x+2} + 2^x}{2^x}$

(c) $\frac{9^{2x}}{3^x}$

$$\frac{2^{4(n+2)} \times 2^n}{2^{5n+3}}$$

$$\frac{2^x(2^2 + 1)}{2^x}$$

$$\frac{(3^2)^{2x}}{3^x}$$

$$\frac{2^{4n+8} \times 2^n}{2^{5n+3}}$$

$$(2^2 + 1)$$

$$\frac{3^{4x}}{3^x}$$

$$\frac{2^{5n+8}}{2^{5n+3}} = 2^5$$

$$= 5$$

$$= 3^{3x}$$

7. (a) $3^{3x+3} = 81$

$$3^{3x+3} = 3^4 \quad (\text{same base on both sides, so base can cancel off})$$

$$3x + 3 = 4 \quad (\text{equate the powers and solve for } x)$$

$$x = \frac{1}{3}$$

(b) $2^{n+3} = 35$

$$n + 3 \log 2 = \log 35$$

$$n + 3 = \frac{\log 35}{\log 2}$$

$$n + 3 = 5.13$$

$$n = 2.13$$

8. (a) $1 + 3 \text{ in mod } 4$

$$4 \text{ mod } 4$$

$$= 0$$

(b) $2 + 1 \text{ mod } 5$

$$2 + (1 \text{ mod } 5)$$

$$2 + 1$$

$$= 3$$

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Solution - Week 1

Year 12

Mathematics

1. $y = x^2 + 3x + 2$

$y = (x + 1)(x + 2)$ (Type 1 factorisation)

x-intercept (y=0)

$(x + 1) = 0$ $(x + 2) = 0$

$x = -1$ $x = -2$

y-intercept (x=0)

$y = x^2 + 3x + 2$

$y = (0)^2 + 3(0) + 2$

$y = 2$

Turning Point (Vertex)

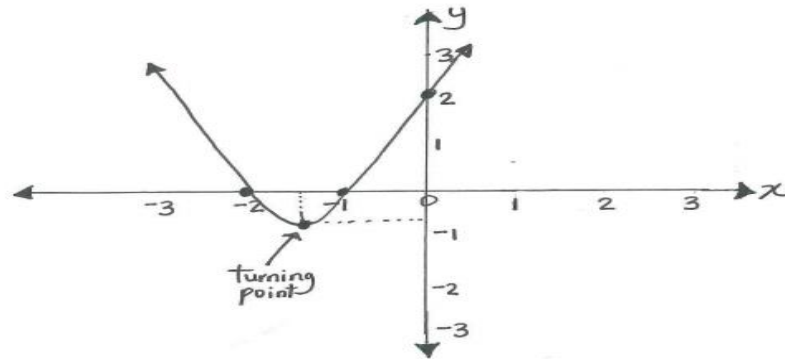
$x = \frac{x_1 + x_2}{2} = \frac{-1 + -2}{2} = -1.5$

$y = x^2 + 3x + 2$

$y = (-1.5)^2 + (-1.5) + 2$

$y = -0.25$

Therefore Turning Point = (-1.5, -0.25)



2. $f(x) = 3x - x^2$

x-intercept (y=0)

$f(x) = x(3 - x)$

$x=0$ $3 - x = 0$

$x = 3$

y-intercept (x=0)

$f(x) = x(3 - x)$

$f(0) = 0(3 - 0)$

$= 0$

Turning Point (Vertex)

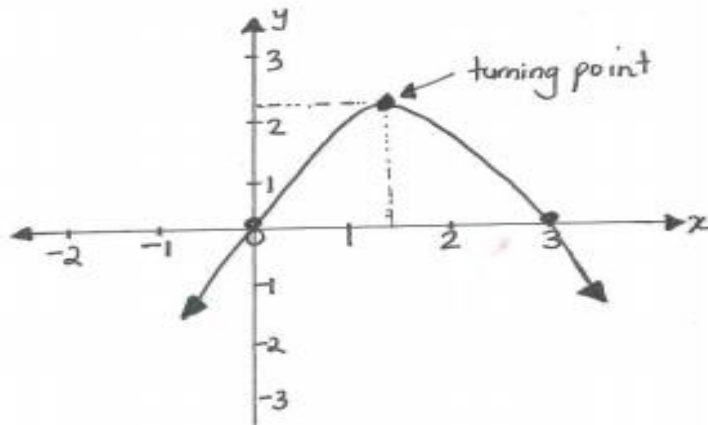
$x = \frac{x_1 + x_2}{2} = \frac{0 + 3}{2} = 1.5$

$f(x) = x(3 - x)$

$f(1.5) = 1.5(3 - 1.5)$

$= 2.25$

Therefore Turning Point = (1.5, 2.25)



3. $y = (2x - 1)(x - 3)$

x-intercept (y=0)

$(2x - 1) = 0$ $(x - 3) = 0$

$x = 0.5$ **$x = 3$**

y-intercept (x=0)

$y = (2x - 1)(x - 3)$

$y = (2(0) - 1)(0 - 3)$

$y = 3$

Turning Point (Vertex)

$x = \frac{x_1 + x_2}{2} = \frac{0.5 + 3}{2} = 1.75$

$y = (2x - 1)(x - 3)$

$y = (2(1.75) - 1)(1.75 - 3)$

$y = -3.125$

Therefore Turning Point = (1.75, -3.125)

