## WORKSHEET 18

SCHOOL: BA SANGAM COLLEGE
SUBJECT: MATHEMATICS

YEAR: 10
NAMEOF STUDENT: $\qquad$

| STRAND | 4- GEOMETRY |  |
| :--- | :--- | :---: |
| SUB-STRAND | 4.5 Intersecting Chord Theorem |  |
| LEARNING OUTCOME | Identify different types and properties of <br>  <br>  <br>  <br>  <br> $\quad$intersecting chords. |  |

## $\underline{\text { Two Chords Intersect in a Circle }}$

If two chords intersect inside a circle then the product of the lengths of the segments of one chord equals the product of the lengths of the segments of the other chord


$$
a \bullet b=c \bullet d
$$

## Theorem Proof:



Given chords AB and CD , prove that
$A E \cdot E C=D E \cdot E B$
$\angle \mathrm{BAC}=\angle \mathrm{BDC}$ as inscribed angles subtended by the same chord BC
$\angle A B D=\angle A C D$ as inscribed angles subtended by the same chord $A D \angle$
$\mathrm{AEB}=\angle \mathrm{DEC}$ as a pair of vertical angles

By Triangles with Two Equal Angles
are Similar we have $\triangle A E B \sim \triangle D E C$.

Thus:

Example Find $x$ in each of the following
(a)

(b)


By Theorem 1, $x \cdot x=2 \cdot 10$

$$
\begin{aligned}
& x^{2}=20 \\
& x=v 20 \\
& x=4.47
\end{aligned}
$$

## EXERCISE

The figure given below shows two chords intersecting inside a circle at $\mathbf{x}$.

(a) Complete the relationship below.

$$
\overline{\mathrm{PX}} \times \square=
$$

$\qquad$ x $\qquad$
(b) If $\overline{P X}=2 \mathrm{~cm}$ and $\overline{Q X}=8 \mathrm{~cm}$, find the length of $\overline{\mathrm{RX}}$.
(3MARKS)
2. For the following, find the value of $X$


