



3055 BA SANGAM COLLEGE

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WORKSHEET 24

School: Ba Sangam College

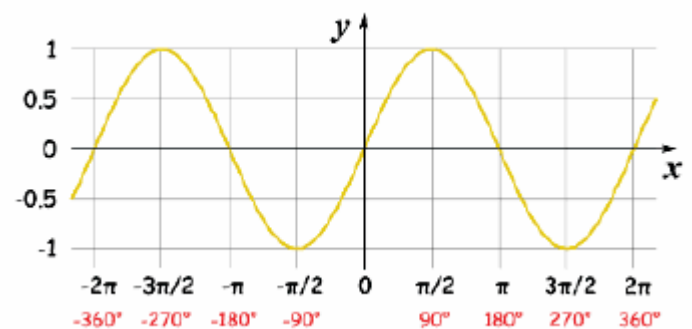
Year / Level: 11

Subject: Mathematics

Name of Student: _____

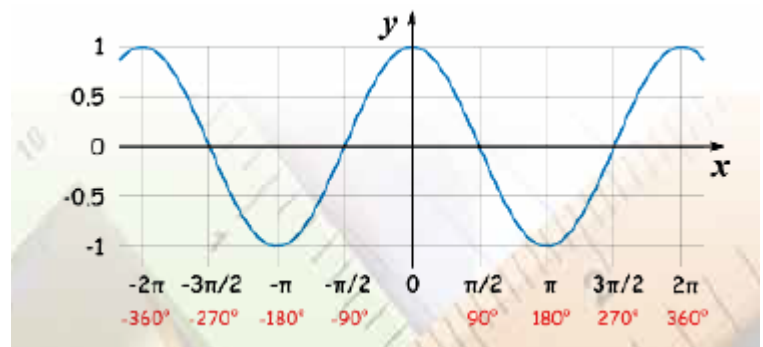
Strand	TRIGONOMETRIC GRAPHS
Sub strand	Sine, Cosine and Tangent Graphs
Content Learning Outcome	To sketch basic trigonometric graphs

Trigonometric	Shape	Period	Range (y values)
$y = \sin x$ $0^\circ \leq x \leq 360^\circ$		360° or 2π radians	$-1 \leq y \leq 1$
$y = \cos x$ $0^\circ \leq x \leq 360^\circ$		360° or 2π radians	$-1 \leq y \leq 1$
$y = \tan x$ $0^\circ \leq x \leq 360^\circ$		180° or π radians	$y \in \mathbb{R}$



Graph of Cosine

Cosine is just like Sine, but it starts at 1 and heads down until π radians (180°) and then heads up again.

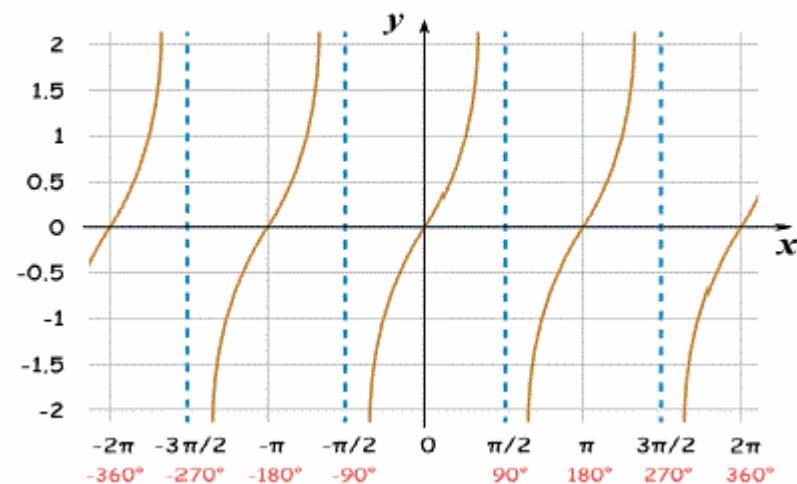


Sine Graph

The Sine Function has this beautiful up-down curve (which repeats every 2π radians, or 360°). It starts at 0, heads up to 1 by $\pi/2$ radians (90°) and then heads down to -1.

Graph of Tangent Function

The Tangent function has a completely different shape ... it goes between negative and positive Infinity, crossing through 0 (every π radians, or 180°), as shown on this plot. At $\pi/2$ radians, or 90° (and $-\pi/2$, $3\pi/2$, etc) the function is officially undefined, because it could be positive Infinity or negative Infinity.



Graph of Sine x - with varying amplitudes

We start with $y = \sin x$.

It has **amplitude** = 1 and **period** = 2π .

Now let's look at the graph of $y = 5 \sin x$.

This time we have amplitude = 5 and period = 2π .

(I have used a different scale on the y -axis.)

And now for $y = 10 \sin x$.

Amplitude = 10 and period = 2π .

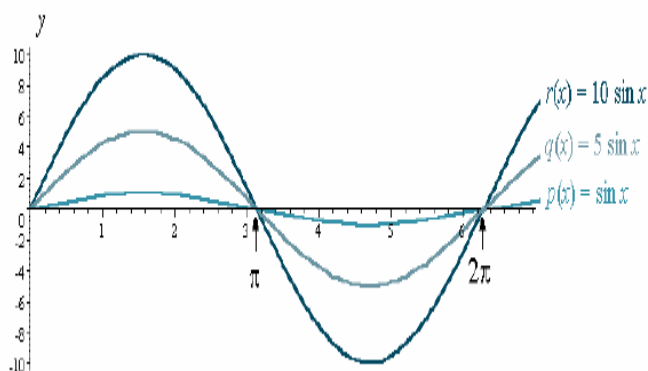
For comparison, and using the same y -axis scale,

here are the graphs of $p(x) = \sin x$, $q(x) = 5 \sin x$

and $r(x) = 10 \sin x$ on the one set of axes.

Note that the graphs have the same **period**

(which is 2π) but different **amplitude**.



Graph of Cosine x - with varying amplitudes

Now let's see what the graph of $y = a \cos x$ looks like. This time the angle is measured from the positive vertical axis.

Now let's have a look at the graph of the simplest cosine curve, $y = \cos x$ ($= 1 \cos x$)

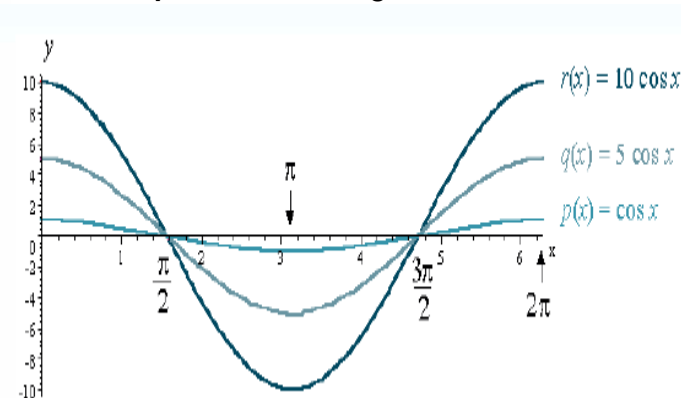
We note that the **amplitude** = 1 and **period** = 2π .

Similar to what we did with $y = \sin x$ above, we now see the graphs of

- $p(x) = \cos x$
- $q(x) = 5 \cos x$
- $r(x) = 10 \cos x$

on one set of axes, for comparison:

Note: For the cosine curve, just like the sine curve, the **period** of each graph is the same (2π), but the **amplitude** has changed



Exercise 1

Sketch the graph of $y = 2 \sin x$

Exercise 2

Sketch the graph of $y = 3 \cos x$